

# Not a subset sum

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            1 second  
Memory limit:         1024 megabytes

We are given an array  $a_0, a_1, \dots, a_{2^n-1}$  of length  $2^n$ . For a string  $q$  of length  $n$  over the alphabet  $0, 1, ?$  (1-indexed), define the "generalized subset sum"  $S(q)$  as the sum of  $a_j$  over all indices  $j$  that satisfy:

- For each  $1 \leq k \leq n$ , if  $q_k = 0$  then the  $k$ -th bit of  $j$  is 0.
- For each  $1 \leq k \leq n$ , if  $q_k = 1$  then the  $k$ -th bit of  $j$  is 1.
- If  $q_k = ?$  there is no restriction on the  $k$ -th bit of  $j$ .

For example, when  $n = 3$  and  $s = 0?1$ , the generalized subset sum is  $S(q) = a_4 + a_6$  (binary 100 and 110). **Note that the first bit is the lowest bit.**

Your task is to compute the generalized subset sum for each string of length  $n$  over the alphabet  $0, 1, ?$ . Because the total output can be large, you only need to output the **bitwise XOR** of all these sums.

## Input

The first line of the input contains an integer  $n$  ( $1 \leq n \leq 16$ ).

The second line of the input contains  $2^n$  integers  $a_0, a_1, \dots, a_{2^n-1}$  ( $0 \leq a_i \leq 9$ ), contents in array  $a$ .

## Output

Print an integer denoting the bitwise-XOR of all generalized subset sums.

## Examples

| standard input | standard output |
|----------------|-----------------|
| 1<br>3 5       | 14              |
| 2<br>2 6 8 8   | 0               |

## Note

The following are query strings  $q$  and their corresponding generalized subset sums  $S(q)$  in **sample 2**:

$$q = 00, S(q) = a_0 = 2$$

$$q = 10, S(q) = a_1 = 6$$

$$q = ?0, S(q) = a_0 + a_1 = 2 + 6 = 8$$

$$q = 01, S(q) = a_2 = 8$$

$$q = 11, S(q) = a_3 = 8$$

$$q = ?1, S(q) = a_2 + a_3 = 16$$

$$q = 0?, S(q) = a_0 + a_2 = 10$$

$$q = 1?, S(q) = a_1 + a_3 = 14$$

$$q = ??, S(q) = a_0 + a_1 + a_2 + a_3 = 24$$

Now it is easy to verify that the output is 0.