

# Bichromatic Cycles

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            10 seconds  
Memory limit:         512 megabytes

You are given an undirected graph. You must color each vertex of the graph in such a way that the following two conditions are met:

- There is no monochromatic cycle<sup>1</sup> in the graph, i.e., there is no cycle whose vertices are all of the same color.
- For each pair of distinct colors  $c_1, c_2$  that appear in the graph, there exists a bichromatic cycle with colors  $c_1$  and  $c_2$ , i.e., there is a cycle that contains at least one vertex of color  $c_1$ , at least one vertex of color  $c_2$ , and no vertices of any other color.

Report whether or not it is possible to do so, and, if it is, provide a valid coloring.

## Input

The first line contains an integer  $T$  ( $1 \leq T \leq 2000$ ), the number of independent test cases to process.

Each case begins with a line containing two integers  $n$  and  $m$  ( $2 \leq n \leq 10^6$ ,  $1 \leq m \leq 3 \cdot 10^6$ ), the number of vertices and the number of edges in the graph, respectively.

This is followed by  $m$  lines, the  $i$ -th of which contains two integers  $u_i$  and  $v_i$  ( $1 \leq u_i, v_i \leq n$ ,  $u_i \neq v_i$ ) — the vertices that the  $i$ -th edge connects. There is at most one edge between every pair of vertices.

The sum of  $(n + m)$  for all cases is at most  $4 \cdot 10^6$ .

## Output

For each case, if there is no valid coloring, print a single line with the word “NO”. Otherwise, print a line with the word “YES” followed by an integer  $C$  ( $1 \leq C \leq n$ ), the number of colors you will use.

Then, print a new line with  $n$  integers between 1 and  $C$ , the  $i$ -th of which is the color assigned to vertex  $i$ . For all  $1 \leq i \leq C$ , there should be no cycle with vertices of color  $i$ , and for all  $1 \leq i < j \leq C$ , there should be a cycle with vertices of colors  $i$  and  $j$ . If there are multiple possible colorings, you can print any of them.

*We strongly recommend using fast I/O for this problem.*

---

<sup>1</sup>A cycle in a graph is a list of distinct vertices  $(v_1, \dots, v_c)$ , where  $c \geq 3$ , such that for all  $1 \leq i < c$  there is an edge between vertices  $v_i$  and  $v_{i+1}$ , and there is also an edge between  $v_c$  and  $v_1$ .

## Example

standard input	standard output
2	YES 3
5 8	1 2 2 3 3
1 2	YES 1
1 3	1 1 1 1
1 4	
2 3	
5 1	
4 3	
4 5	
5 2	
4 2	
1 2	
3 4	

## Note

The figure below shows one possible coloring for the first example. There are no cycles with vertices of the same color, and, for each pair of colors, there exists a cycle with just those two colors: for colors 1 and 2, the cycle is (1, 2, 3); for colors 1 and 3, it is (1, 4, 5); and for colors 2 and 3, it is (2, 3, 4, 5).

